

Giải bài 3 trang 154 sgk toán Đại Số lớp 10

Đề bài:

Rút gọn biểu thức

a) $\sin(a + b) + \sin\left(\frac{\pi}{2} - a\right) \sin(-b)$.

b) $\cos\left(\frac{\pi}{4} + a\right) \cos\left(\frac{\pi}{4} - a\right) + \frac{1}{2} \sin^2 a$

c) $\cos\left(\frac{\pi}{2} - a\right) \sin\left(\frac{\pi}{2} - b\right) - \sin(a - b)$

Đáp án:

a) $\sin(a + b) + \sin\left(\frac{\pi}{2} - a\right) \sin(-b)$
 $= \sin a \cos b + \cos a \sin b - \cos a \sin b$
 $= \sin a \cos b$.

b) $\cos\left(\frac{\pi}{4} + a\right) \cos\left(\frac{\pi}{4} - a\right) + \frac{1}{2} \sin^2 a$
 $= \frac{1}{2} \cos\left[\frac{\pi}{4} + a + \frac{\pi}{4} - a\right] + \frac{1}{2} \cos\left[\left(\frac{\pi}{4} + a\right) - \left(\frac{\pi}{4} - a\right)\right] + \frac{1}{2} \left(\frac{1 - \cos 2a}{2}\right)$
 $= \frac{1}{2} \cos 2a + \frac{1}{4} (1 - \cos 2a)$
 $= \frac{1 + \cos 2a}{4} = \frac{1}{2} \cos^2 a$.

c) $\cos\left(\frac{\pi}{2} - a\right) \sin\left(\frac{\pi}{2} - b\right) - \sin(a - b)$
 $= \sin a \cos b - \sin a \cos b + \sin b \cos a$
 $= \sin b \cos a$.