

Giải bài 1 trang 153 sgk toán Đại Số lớp 10

Đề bài: Tính

a) $\cos 225^0$, $\sin 240^0$, $\cot(-15^0)$, $\tan 75^0$;

b) $\sin \frac{7\pi}{12}$, $\cos(-\frac{\pi}{12})$, $\tan(\frac{13\pi}{12})$

Đáp án:

$$\begin{aligned} \text{a) } \cos 225^0 &= \cos(180^0 + 45^0) = -\cos 45^0 \\ &= -\frac{\sqrt{2}}{2} \end{aligned}$$

$$\begin{aligned} \text{+) } \sin 240^0 &= \sin(180^0 + 60^0) \\ &= -\sin 60^0 = -\frac{\sqrt{3}}{2} \end{aligned}$$

$$\begin{aligned} \text{+) } \cot(-15^0) &= -\cot 15^0 \\ &= -\tan 75^0 = -\tan(30^0 + 45^0) \\ &= \frac{-\tan 30^0 - \tan 45^0}{1 - \tan 30^0 \tan 45^0} \\ &= \frac{-\frac{1}{\sqrt{3}} - 1}{1 - \frac{1}{\sqrt{3}}} = -\frac{\sqrt{3}+1}{\sqrt{3}-1} = -\frac{(\sqrt{3}+1)^2}{2} \\ &= -2 - \sqrt{3} \end{aligned}$$

$$\text{+) } \tan 75^0 = \cot 15^0 = 2 + \sqrt{3}$$

$$\text{b) } \sin \frac{7\pi}{12} = \sin\left(\frac{\pi}{3} + \frac{\pi}{4}\right)$$

$$= \sin \frac{\pi}{3} \cos \frac{\pi}{4} + \cos \frac{\pi}{3} \sin \frac{\pi}{4}$$

$$= \frac{\sqrt{2}}{2} \left(\frac{\sqrt{3}}{2} + \frac{1}{2} \right) = \frac{\sqrt{6} + \sqrt{2}}{4}$$

$$\text{+) } \cos\left(-\frac{\pi}{12}\right) = \cos\left(\frac{\pi}{4} - \frac{\pi}{3}\right)$$

$$= \cos \frac{\pi}{4} \cos \frac{\pi}{3} + \sin \frac{\pi}{3} \sin \frac{\pi}{4}$$

$$= \frac{\sqrt{2}}{2} \left(\frac{\sqrt{3}}{2} + \frac{1}{2} \right) = 0,9659$$

$$\text{+) } \tan\left(\frac{13\pi}{12}\right) = \tan\left(\pi + \frac{\pi}{12}\right)$$

$$= \tan \frac{\pi}{12} = \tan\left(\frac{\pi}{3} - \frac{\pi}{4}\right)$$

$$= \frac{\tan \frac{\pi}{3} - \tan \frac{\pi}{4}}{1 + \tan \frac{\pi}{3} \tan \frac{\pi}{4}} = \frac{\sqrt{3} - 1}{1 + \sqrt{3}} = 2 - \sqrt{3}$$